

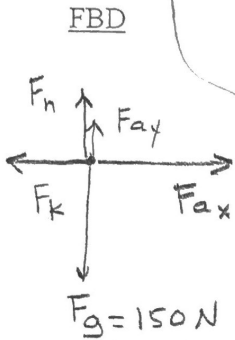
$\Sigma F = ma$

$F_g = mg$

$F_k = \mu_k F_n$

Name _____

Forces Problem Set # 7: Pulling/Pushing at an Angle

Draw a complete FBD (x and y forces) and write the ΣF_y and ΣF_x for each problem to get full credit.Ex: A passenger is pulling on the strap of a 15.0 kg suitcase with a force of 69.0 N. The strap makes an angle of 37.5° with the horizontal. The coefficient of friction $\mu_k = 0.25$. Find the normal force and the acceleration of the suitcase.

$$\Sigma F_y \quad \Sigma F_x$$

$$F_n + F_{ay} = F_g \quad F_{ax} - F_k = ma$$

$$F_n = F_g - F_{ay}$$

$$= 150 \text{ N} - 69 \text{ N} (\sin 37.5^\circ)$$

$$= 108 \text{ N}$$

$$a = \frac{F_{ax} - F_k}{m}$$

$$= \frac{69 \text{ N} (\cos 37.5^\circ) - 0.25 (108 \text{ N})}{15 \text{ kg}}$$

$$= \frac{54.7 \text{ N} - 27 \text{ N}}{15 \text{ kg}}$$

$$= \boxed{1.85 \text{ m/s}^2 \text{ right}}$$

1. A 15 kg sled is being pulled across a horizontal surface at a constant velocity. The pulling force F_a has a magnitude of 83.5 N and is directed at an angle of 30° above the horizontal. Find the normal force and the coefficient of kinetic friction. (Note: just as in the example, F_n is not equal to F_g ; you have to use the ΣF_y equation first.)

FBD

 ΣF_y ΣF_x

$$F_n + F_{ay} = F_g \quad F_{ax} = F_k$$

$$F_n = F_g - F_{ay}$$

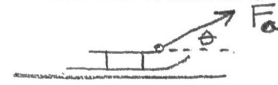
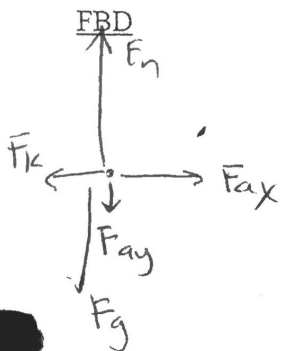
$$= 150 \text{ N} - 83.5 \text{ N} (\sin 30^\circ)$$

$$= 108 \text{ N}$$

$$F_k = 83.5 \text{ N} \cos 30^\circ$$

$$= 72 \text{ N}$$

$$\mu_k = \frac{F_k}{F_n} = \frac{72 \text{ N}}{108 \text{ N}} = .67$$

2. A box of books weighing 325 N accelerates across the floor when the box is pushed with a force of 425 N exerted downward at an angle of 35° below the horizontal. The coefficient of friction $\mu_k = 0.35$. Find the normal force and the acceleration of the box.

$$\Sigma F_y \quad \Sigma F_x$$

$$F_n = F_g + F_{ay}$$

$$F_n = 325 \text{ N} + 425 \text{ N} \sin 35^\circ$$

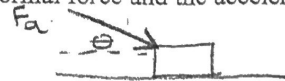
$$= 569 \text{ N}$$

$$F_{ax} - F_k = ma$$

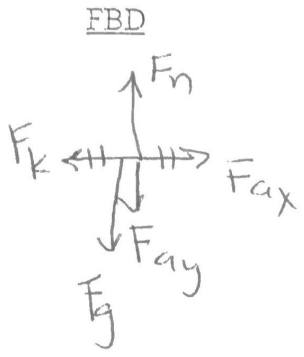
$$348 \text{ N} - .35 (569 \text{ N}) = ma$$

$$348 \text{ N} - 199 \text{ N} = ma$$

$$a = \frac{149 \text{ N}}{32.5 \text{ kg}} = 4.6 \text{ m/s}^2$$



3. A person pushes a 14.0 kg lawn mower at constant speed with a force of $F_a = 88.0 \text{ N}$ directed along the handle, which is at an angle of 45 degrees to the horizontal. Find F_k , F_n , and μ_k .



$$\Sigma F_y$$

$$\Sigma F_x$$

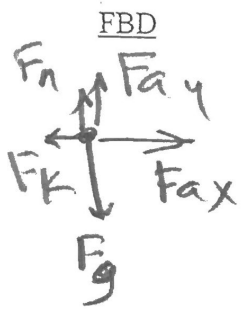
$$F_{ix} = F_k$$

$$F_{ax} = F_a \cos \theta = 62 \text{ N} = F_k$$

$$F_n = F_g + F_{ay} = 140 \text{ N} + 88 \text{ N}(\sin 45) = 202 \text{ N}$$

$$\mu_k = \frac{F_k}{F_n} = .31$$

4. A 10.0 kg box is pulled along a horizontal surface a $F_a = 40.0 \text{ N}$ applied at a 30 degree angle above the horizontal. $\mu_k = 0.3$. Calculate the acceleration.



$$\Sigma F_y$$

$$\Sigma F_x$$

$$F_{ay} + F_n - F_g = 0 \quad F_{ax} - F_k = ma$$

$$F_n = F_g - F_{ay} = 100 \text{ N} - 20 \text{ N}$$

$$F_n = 80 \text{ N}$$

$$F_k = \mu_k F_n = 24 \text{ N}$$

$$a = \frac{\Sigma F}{m} = \frac{34.6 \text{ N} - 24 \text{ N}}{10 \text{ kg}}$$

$$F_n = 80 \text{ N}$$

$$F_k = 24 \text{ N}$$

$$a = 1.06 \text{ m/s}^2$$